

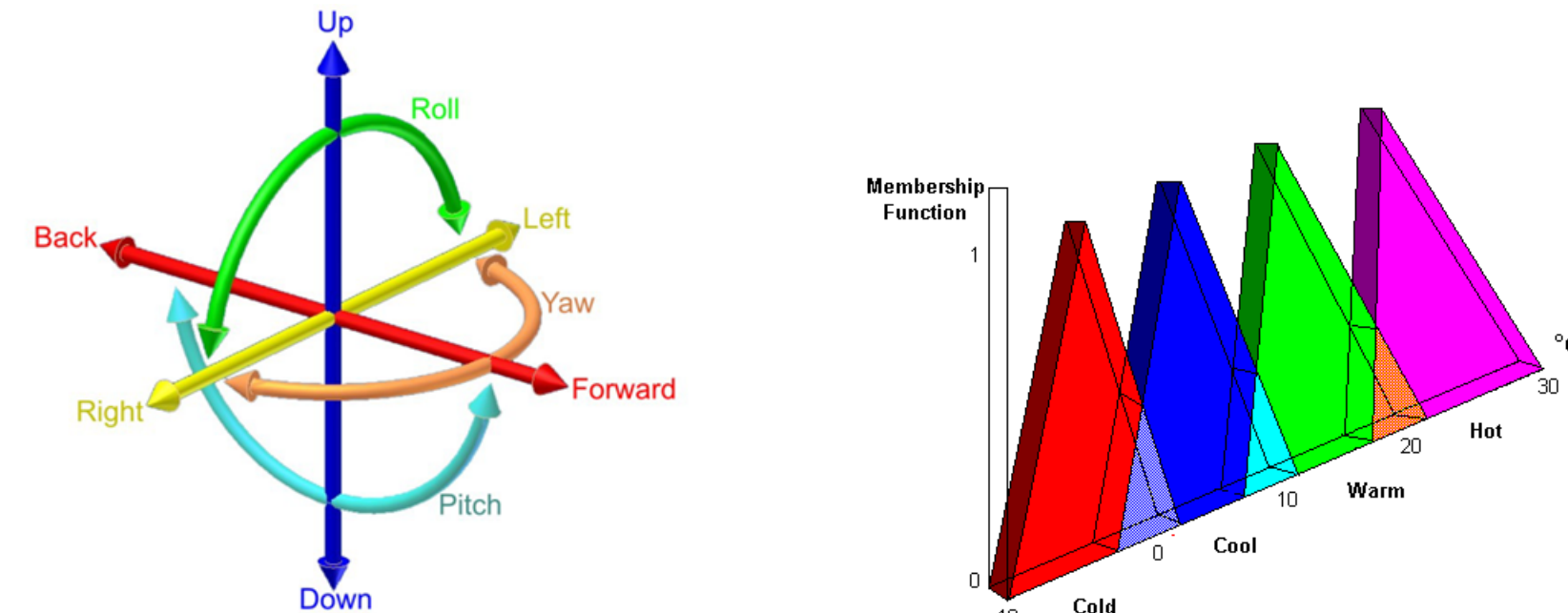
Multi-Input Multi-Output (MIMO) Adaptive Control of 9-DOF Hyper-Redundant Robotic Arm

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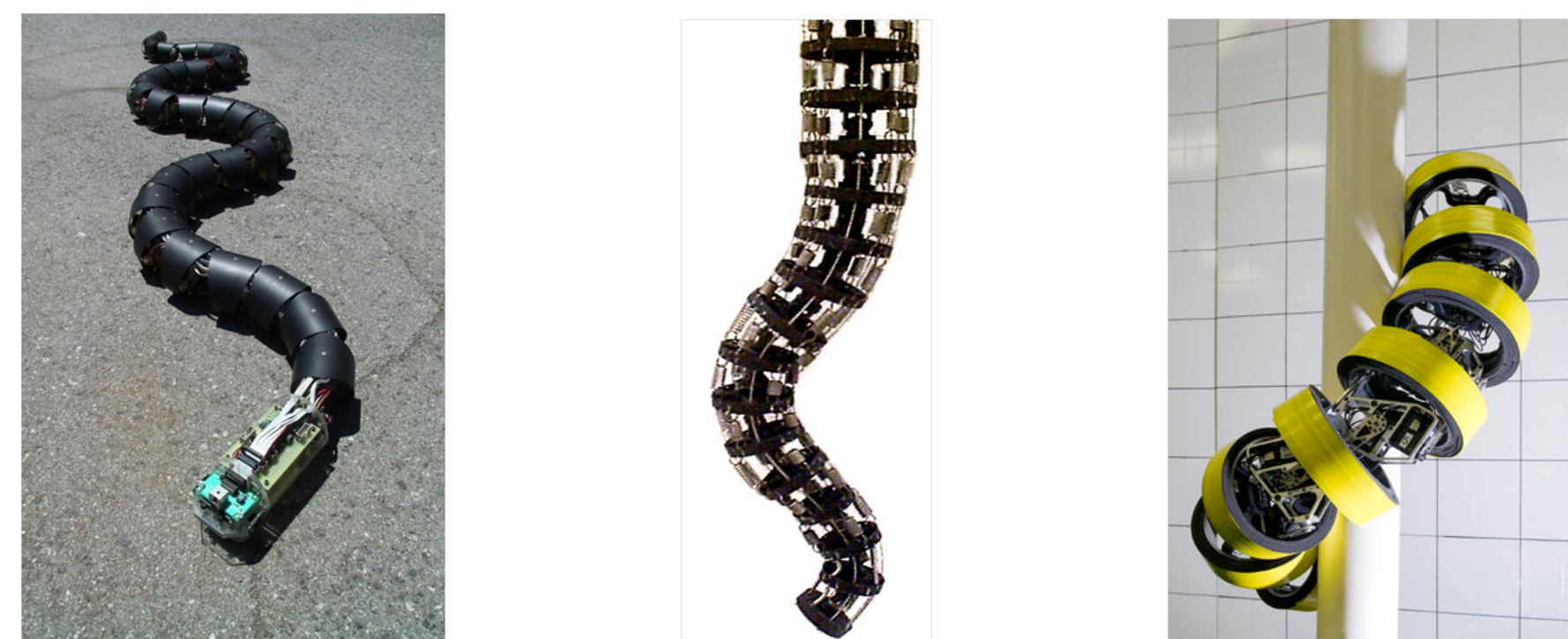
KEY WORDS

- ▶ **Degree of freedom (DOF) and Fuzzy system**



(a) Degree of freedom (b) Fuzzy system

- ▶ **Hyper-redundant robots (HRR)**



(a) Snake (b) Elephant trunk (c) Tentacle

DYNAMIC MODEL

- **Manipulator Jacobian Matrix:** An expression to connect angular velocity ω_n^0 , linear velocity v_n^0 of the end-effector and joint velocity \dot{q} as

$$\begin{aligned}\omega_n^0 &= J_\omega \dot{q}, \\ v_n^0 &= J_v \dot{q},\end{aligned}$$

where J_ω and J_v are $3 \times n$ matrices.

- Euler-Lagrange Equation:

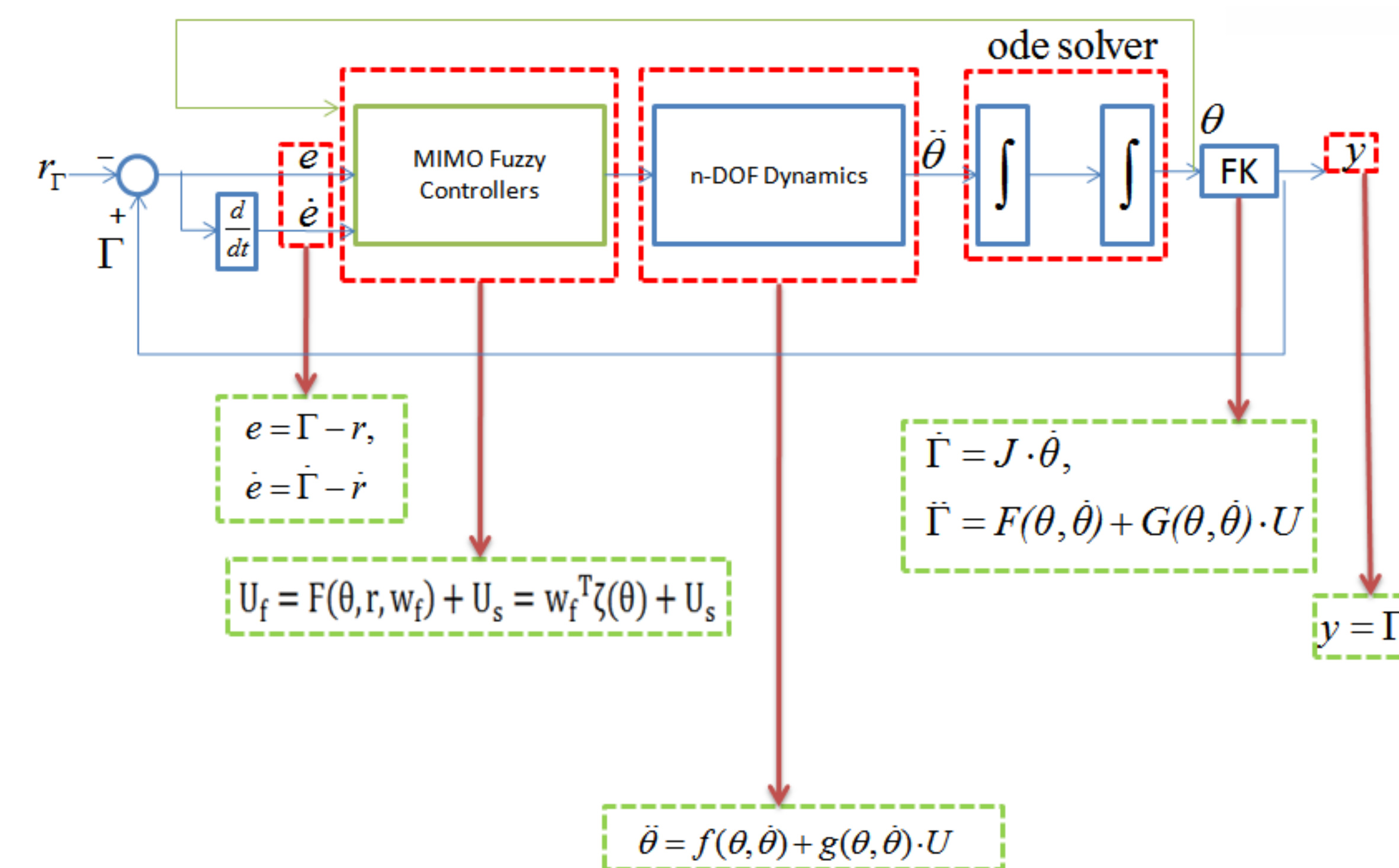
$$\frac{d}{dt} \frac{\partial L}{\partial \dot{q}_i} - \frac{\partial L}{\partial q_i} = \tau_i, i = 1, \dots, n,$$

where τ_i is input torque of each motor and the Lagrangian L is given by

$$L = K - P,$$

where K is the kinetic energy and P is the potential energy.

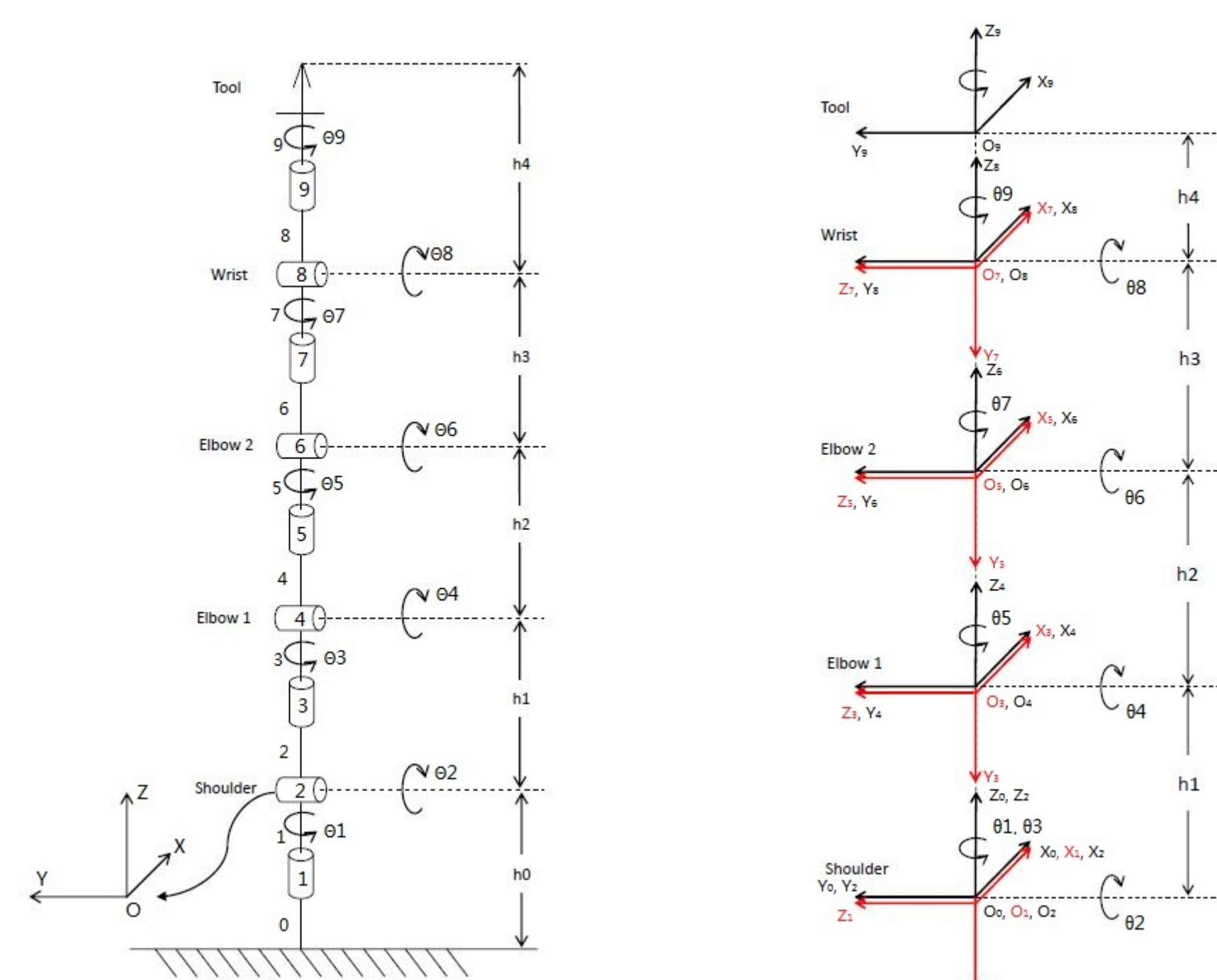
MIMO Adaptive Control in Workspace



OBJECTIVE

- Design both the kinematic and dynamic model of a 9-DOF hyper-redundant arm;
- Apply MIMO adaptive controllers to control the end-effector of the arm in work space.

KINEMATIC MODEL



(a) Joint schematic (b) Frame assignment

EXTRA CONSTRAINTS

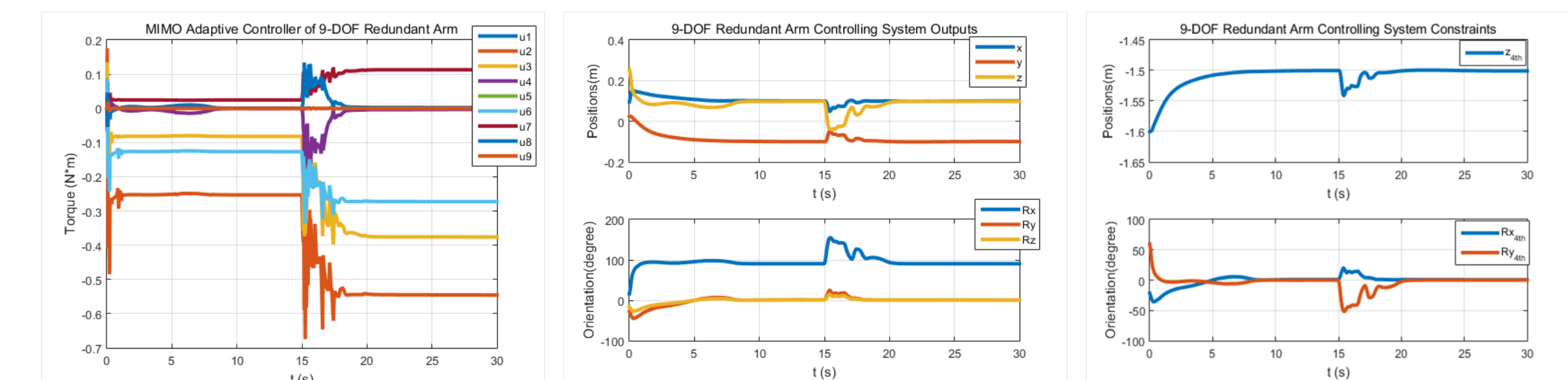
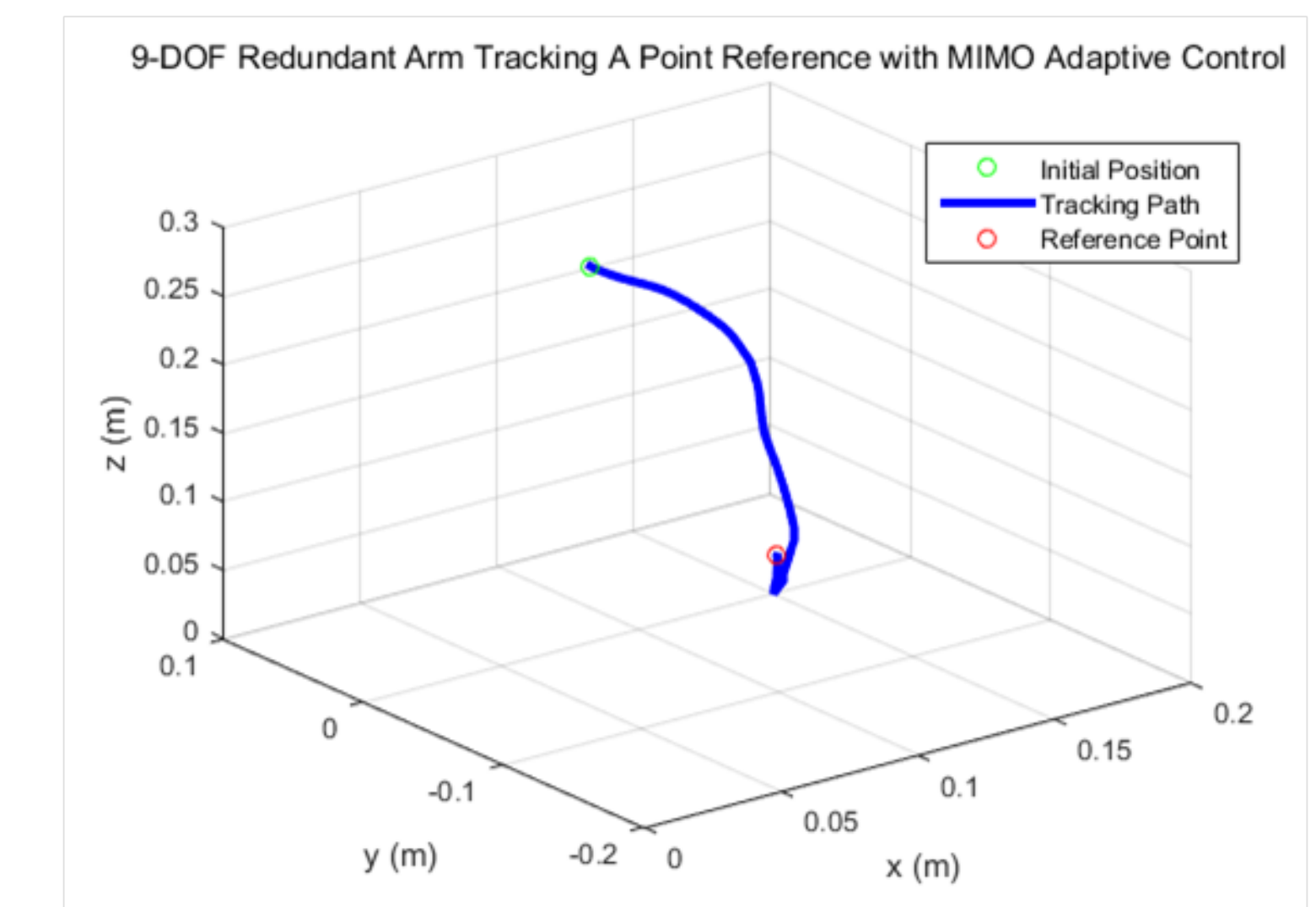
$$\begin{bmatrix} \dot{X} \\ \dot{Y} \\ \dot{Z} \\ \dot{R}_x \\ \dot{R}_y \\ \dot{R}_z \end{bmatrix} = \begin{bmatrix} \text{Jacobian} \\ 6 \times n \end{bmatrix} \cdot \begin{bmatrix} \dot{\theta}_1 \\ \vdots \\ \dot{\theta}_n \end{bmatrix}$$
 +
 [Constraint Jacobian]

Constraints

More redundant!

SIMULATION RESULTS

- ### ► 9-DOF Arm Tracking and Disturbance Simulation



(a) Controllers

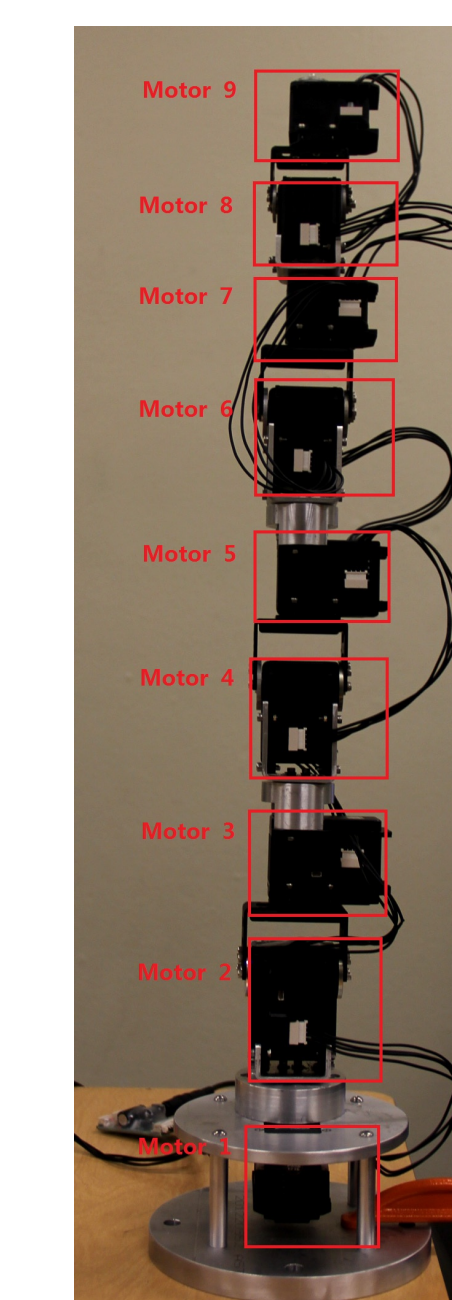
(b) Outputs

(c) Constraints

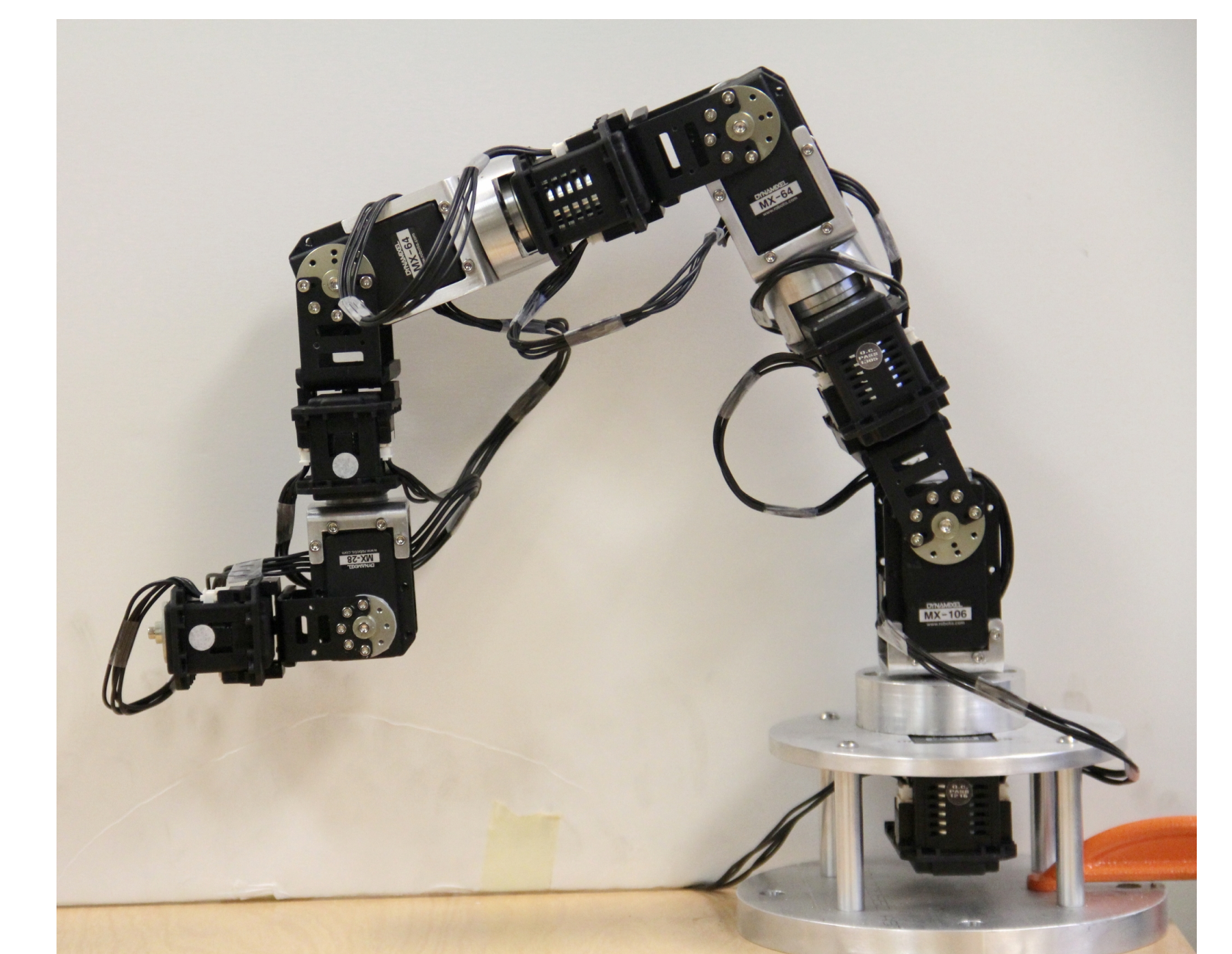
CONCLUSION

- ▶ Take care of the system nonlinearity and uncertainty;
- ▶ Approximate the ideal controller online to the particular system;
- ▶ Adjust itself and try to track the reference again after having system disturbance.

REAL 9-DOF ARM PLATFORM



(a) Home position 1



(b) Home position 2